

Kouamé Y.A.G., Millan M., N'Dri A.B., Charles-Dominique T., Konan M., Bakayoko A., Gignoux J. (2022). Multispecies allometric equations for shrubs and trees biomass prediction in a Guinean savanna (West Africa). Silva Fennica vol. 56 no. 2 article id 10617. <https://doi.org/10.14214/sf.10617>.

Supplementary file S5

Text 1. Output of the stepwise selection of variables for predicting AGB in both trees and shrubs

```
> model11 <- lm(log(AGB) ~ log(H) + log(rDb2H) + log(S.S) + log(n), data = data1)
> summary(model11)

Call:
lm(formula = log(AGB) ~ log(H) + log(rDb2H) + log(S.S) + log(n),
    data = data1)

Residuals:
      Min        1Q     Median        3Q       Max
-1.26444 -0.32288  0.01185  0.37849  1.86875

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -3.36496   0.19790 -17.003 <2e-16 ***
log(H)       0.01670   0.16424   0.102  0.9191
log(rDb2H)   0.99936   0.08243  12.124 <2e-16 ***
log(S.S)    -0.07731   0.08705  -0.888  0.3756
log(n)       0.24651   0.10086   2.444  0.0155 *
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Signif. codes:  0 ‘***’ 0.001 ‘**’ 0.01 ‘*’ 0.05 ‘.’ 0.1 ‘ ’ 1

Residual standard error: 0.5401 on 185 degrees of freedom
Multiple R-squared:  0.9146, Adjusted R-squared:  0.9127
F-statistic: 495.3 on 4 and 185 DF,  p-value: < 2.2e-16

> step(model11) -> final.model

Start:  AIC=-229.15
log(AGB) ~ log(H) + log(rDb2H) + log(S.S) + log(n)

          Df Sum of Sq    RSS    AIC
- log(H)    1   0.003 53.967 -231.14
- log(S.S)  1   0.230 54.194 -230.34
<none>           53.964 -229.15
- log(n)    1   1.743 55.707 -225.12
- log(rDb2H) 1   42.880 96.844 -120.05

Step:  AIC=-231.14
log(AGB) ~ log(rDb2H) + log(S.S) + log(n)

          Df Sum of Sq    RSS    AIC
- log(S.S)  1   0.268 54.236 -232.20
<none>           53.967 -231.14
- log(n)   1   1.911 55.878 -226.53
- log(rDb2H) 1   91.495 145.463  -44.75

Step:  AIC=-232.2
log(AGB) ~ log(rDb2H) + log(n)
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          Df Sum of Sq   RSS   AIC
<none>                 54.24 -232.20
- log(n)      1     3.52  57.76 -222.25
- log(rDb2H)  1   432.75 486.99  182.83

> summary(final.model)

Call:
lm(formula = log(AGB) ~ log(rDb2H) + log(n), data = data1)

Residuals:
    Min      1Q  Median      3Q      Max 
-1.27931 -0.33148  0.01142  0.38381  1.83555 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -3.50230   0.13703 -25.559 < 2e-16 ***
log(rDb2H)   0.95647   0.02476  38.628 < 2e-16 ***
log(n)       0.16815   0.04826   3.485 0.000614 ***  
---
Signif. codes:  0 ‘***’ 0.001 ‘**’ 0.01 ‘*’ 0.05 ‘.’ 0.1 ‘ ’ 1
Residual standard error: 0.5385 on 187 degrees of freedom
Multiple R-squared:  0.9142, Adjusted R-squared:  0.9132 
F-statistic: 995.8 on 2 and 187 DF,  p-value: < 2.2e-16

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Text 2. Output of the stepwise selection of variables for predicting BGB in both trees and shrubs

```

> model2 <- lm(log(BGB) ~ log(H) + log(rDb2H) + log(S.S) + log(n), data =
  data1)

> summary(model2)

Call:
lm(formula = log(BGB) ~ log(H) + log(rDb2H) + log(S.S) + log(n),
  data = data1)

Residuals:
    Min      1Q  Median      3Q      Max 
-1.18384 -0.45903 -0.02269  0.41262  2.26860 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -2.71614   0.22117 -12.281 < 2e-16 ***
log(H)       -0.18478   0.18355  -1.007 0.315383  
log(rDb2H)   0.87770   0.09212   9.528 < 2e-16 ***
log(S.S)    -0.08398   0.09729  -0.863 0.389168  
log(n)       0.43322   0.11272   3.843 0.000167 ***  
---
Signif. codes:  0 ‘***’ 0.001 ‘**’ 0.01 ‘*’ 0.05 ‘.’ 0.1 ‘ ’ 1
Residual standard error: 0.6036 on 185 degrees of freedom
Multiple R-squared:  0.8319, Adjusted R-squared:  0.8282 
F-statistic: 228.8 on 4 and 185 DF,  p-value: < 2.2e-16

> step(model2) -> final.model

Start:  AIC=-186.91
log(BGB) ~ log(H) + log(rDb2H) + log(S.S) + log(n)

          Df Sum of Sq   RSS   AIC
- log(S.S)      1     0.271  67.673 -188.14
- log(H)        1     0.369  67.771 -187.87
<none>                    67.402 -186.91
- log(n)        1     5.382  72.784 -174.31

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- log(rDb2H) 1 33.075 100.477 -113.05

Step: AIC=-188.14
log(BGB) ~ log(H) + log(rDb2H) + log(n)
      Df Sum of Sq   RSS   AIC
- log(H)     1    0.227  67.900 -189.507
<none>          67.673 -188.144
- log(n)     1   15.070  82.743 -151.944
- log(rDb2H) 1   80.189 147.862  -41.641

Step: AIC=-189.51
log(BGB) ~ log(rDb2H) + log(n)

      Df Sum of Sq   RSS   AIC
<none>          67.90 -189.51
- log(n)     1   15.026  82.93 -153.52
- log(rDb2H) 1   285.178 353.08  121.74

> summary(final.model)

Call:
lm(formula = log(BGB) ~ log(rDb2H) + log(n), data = data1)

Residuals:
    Min      1Q  Median      3Q      Max 
-1.16474 -0.45081 -0.00847  0.37699  2.25729 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -2.79325   0.15332 -18.218 < 2e-16 ***
log(rDb2H)   0.77644   0.02771  28.025 < 2e-16 ***
log(n)       0.34733   0.05399   6.433 1.02e-09 ***
---
Signif. codes:  0 ‘***’ 0.001 ‘**’ 0.01 ‘*’ 0.05 ‘.’ 0.1 ‘ ’ 1

Residual standard error: 0.6026 on 187 degrees of freedom
Multiple R-squared:  0.8306, Adjusted R-squared:  0.8288 
F-statistic: 458.5 on 2 and 187 DF,  p-value: < 2.2e-16

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Table 1. Results of ANCOVA test highlighting the influence of the species, of the quantitative explanatory variables ($w = \rho D_b^2 H$ in $\text{g cm}^{-1} \text{m}$, n = total number of stems) and their interaction on the estimation of the aboveground and belowground biomass (AGB and BGB) under models fitted in this study from trees and shrubs measurements in the savanna of the Lamto Scientific Reserve. For trees, D_b (cm) corresponds to the stem basal diameter and H (m) represents the total height in the term $\rho D_b^2 H$. For shrubs, the term $D_b^2 H$ corresponds to the sum of $d_i^2 h_i$ ($i=1\dots n$) of the n stems, where d_i (cm) and h_i (m) are respectively the basal diameter and the total height of each stem. ρ (g cm^{-3}) is the woody specific density.

		Source of variation	Mean Sq	F value	Pr (>F)
AGB	Trees	Species	1.64	6.62	< 0.001***
		ln(w)	285.48	1151.46	< 0.001***
		Species: ln(w)	0.89	3.59	< 0.05*
	Shrubs	Species	0.33	4.93	< 0.01**
		ln(w)	53.43	800.39	< 0.001***
		ln(n)	11.37	170.26	< 0.001***
BGB	Trees	Species: ln(w)	0.23	3.45	< 0.05*
		Species: ln(n)	1.16	17.45	< 0.001***
		Species	3.98	16.15	< 0.001***
	Shrubs	ln(w)	158.34	642.04	< 0.001***
		Species: ln(w)	0.67	2.72	< 0.05*
		Species	1.18	6.97	< 0.01**
		ln(w)	67.51	397.52	< 0.001***
		ln(n)	11.90	70.04	< 0.001***
		Species: ln(w)	0.58	3.41	< 0.05*
		Species: ln(n)	0.98	5.78	< 0.01**

Table 2. Results of ANCOVA test highlighting the influence of the growth form and species, on the relation between height (m) and stem basal diameter (D_b , cm).

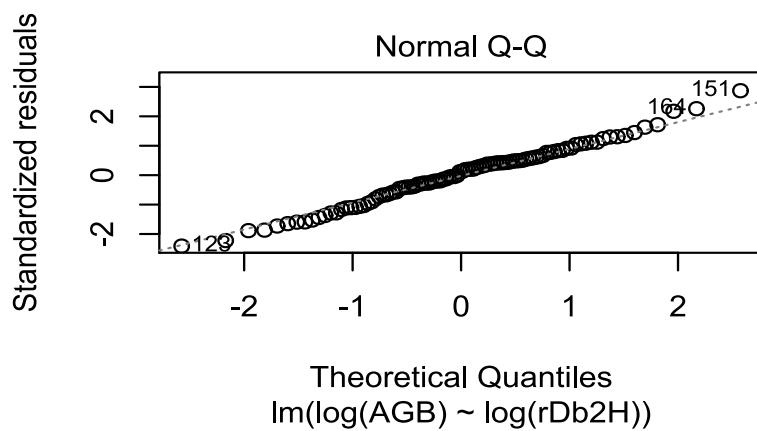
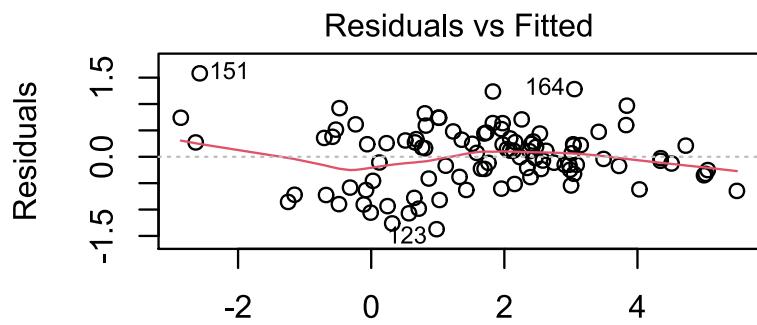
		Dependent variables	Source of variation	Mean Sq	F value	P value
Trees + Shrubs	log (H)		log(D_b)	719.44	2853.56	< 0.001***
			Growth-form	30.72	121.86	< 0.001***
			Species	2.86	11.34	< 0.001***
			D_b : Growth-form	81.60	323.667	< 0.001***
			D_b : Species	3.34	13.24	< 0.001***

Table 3. Values of the wood specific gravity (g cm^{-3}) of each species in this study and in Ifo et al. (2018) study.

Species	Growth form	Wood specific gravity (g cm^{-3})
Species of this study		
<i>Annona senegalensis</i>	Multistemmed shrub	0.499
<i>Bridelia ferruginea</i>	Single stemmed tree	
	Multistemmed shrub	0.640
<i>Crossopteryx febrifuga</i>	Single stemmed tree	0.724
<i>Cussonia arborea</i>	Single stemmed tree	0.399
<i>Piliostigma thonningii</i>	Single stemmed tree	
	Multistemmed shrub	0.665
Species of Ifo et al. study		
<i>Annona senegalensis</i>	Single stemmed shrub	0.487
<i>Bridelia ferruginea</i>	Single stemmed tree	0.610
<i>Crossopteryx febrifuga</i>	Single stemmed tree	0.579
<i>Hymenocardia acida</i>	Single stemmed tree	0.622
<i>Syzygium guineense</i>	Single stemmed tree	0.600

Fig. 1. Quantiles distributions in AGB predicting model of trees

Normal probability (Q-Q) plot and other quantile distributions that assess goodness of fit of the model predicting the total aboveground biomass (AGB) of trees as a function of variable $w = \rho D_b^2 H$, where ρ (g cm⁻³) is the specific woody density, D_b (cm) corresponds to the stem basal diameter of one individual or sample, H (m) represents the total height. In case of a good fit, as is the case here, the residual quantiles should be symmetrically distributed (i.e., with equal variance) around an average = 0 and the plot of theoretical quantiles and quantiles from the fitted sample should lie on a line $y=x$.



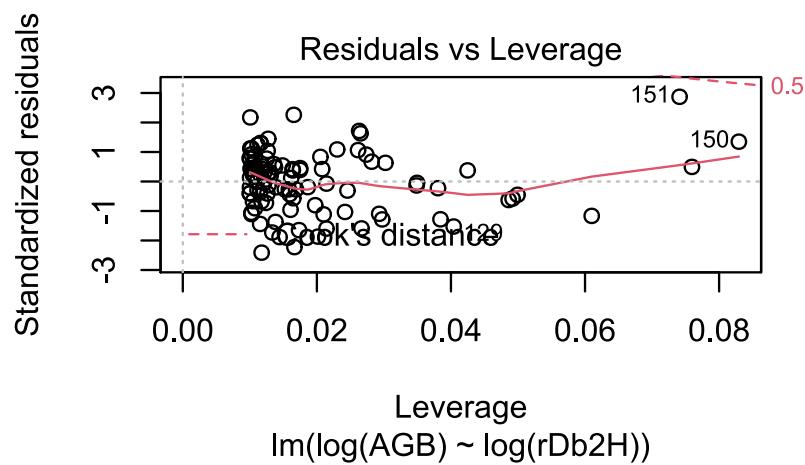
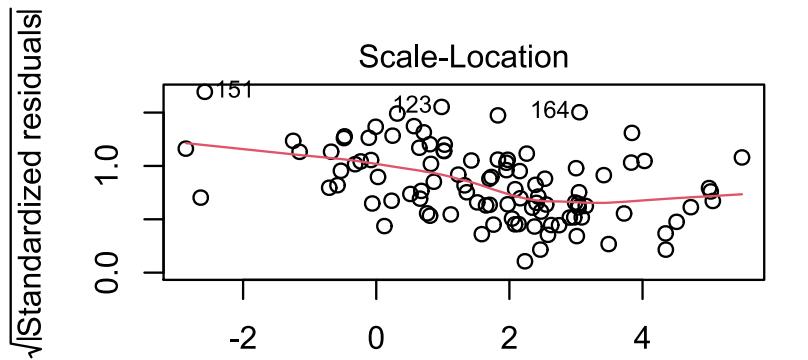
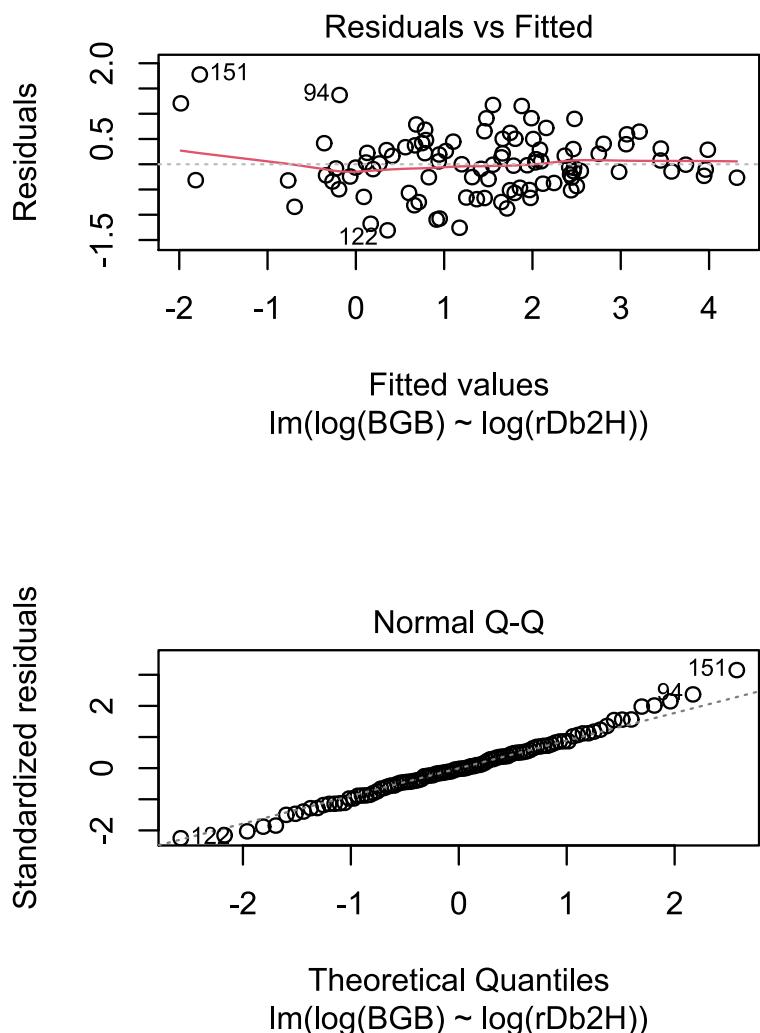


Fig. 2. Quantiles distributions in BGB predicting model of trees

Normal probability (Q-Q) plot and other quantile distributions that assess goodness of fit of the model predicting the total aboveground biomass (BGB) of trees as a function of variable $w = \rho D_b^2 H$.



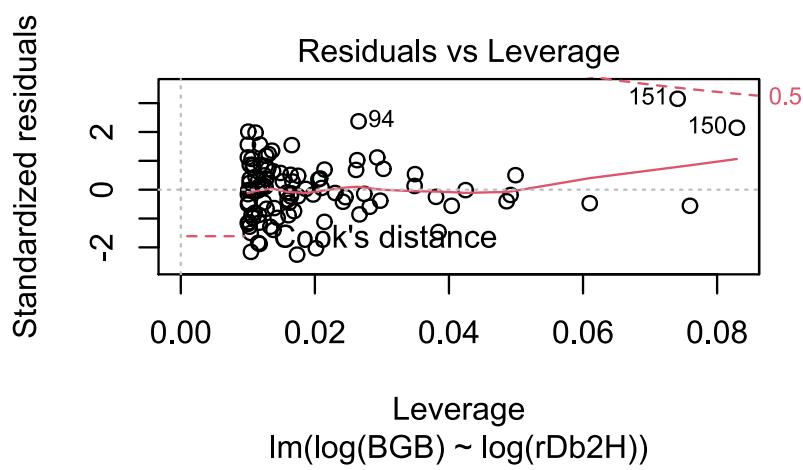
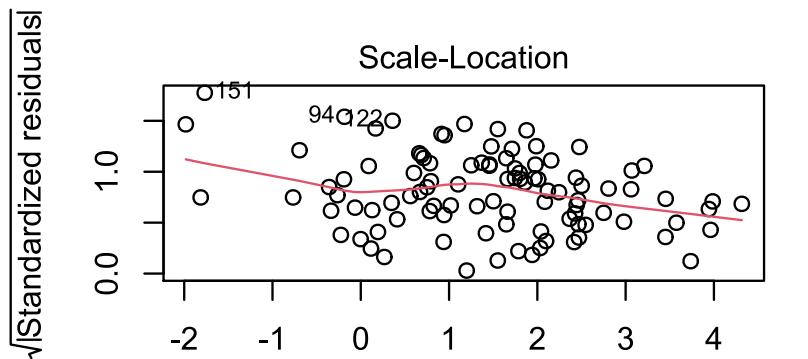
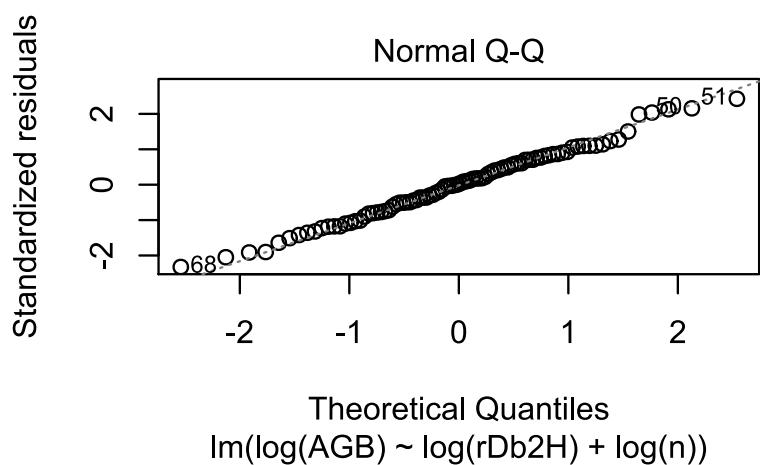
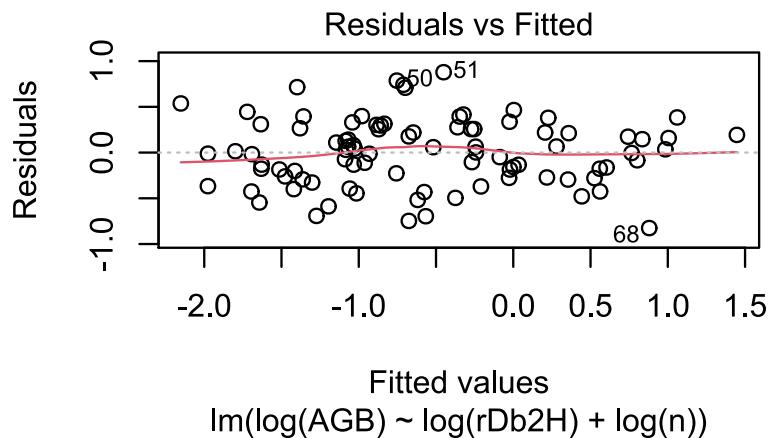


Fig. 3. Quantiles distributions in AGB predicting model of shrubs

Normal probability (Q-Q) plot and other quantile distributions that assess goodness of fit of the model predicting the total aboveground biomass (AGB) of shrubs as a function of variable $w = \rho D_b^2 H$ and n = the total number of stems for one shrub. $D_b^2 H$ corresponds to the sum of $d_i^2 h_i$ ($i=1\dots n$) of the n stems (with d_i = basal diameter in cm and h_i = total height of each stem in m)



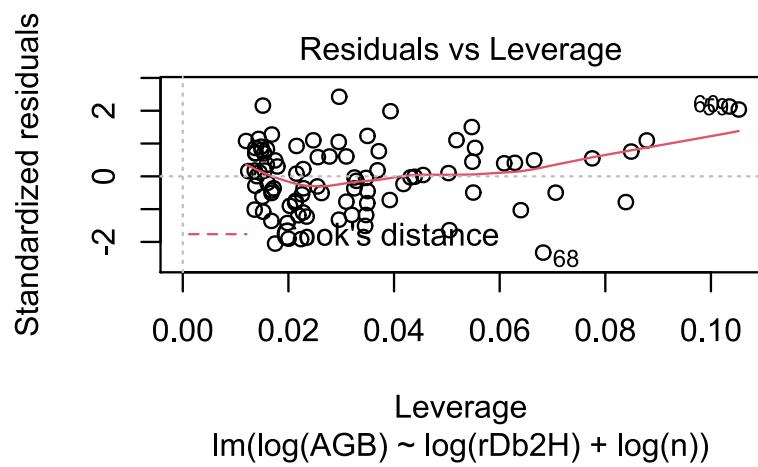
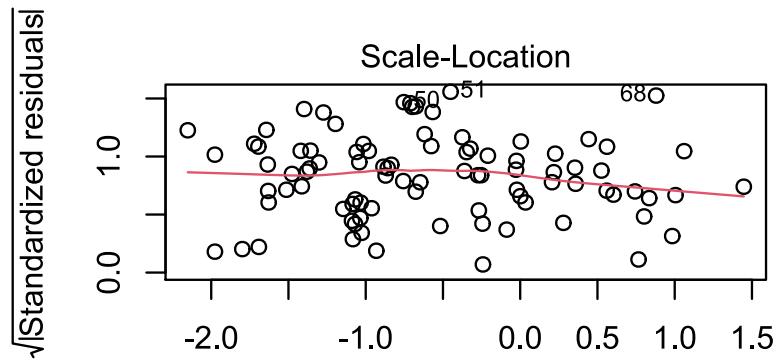
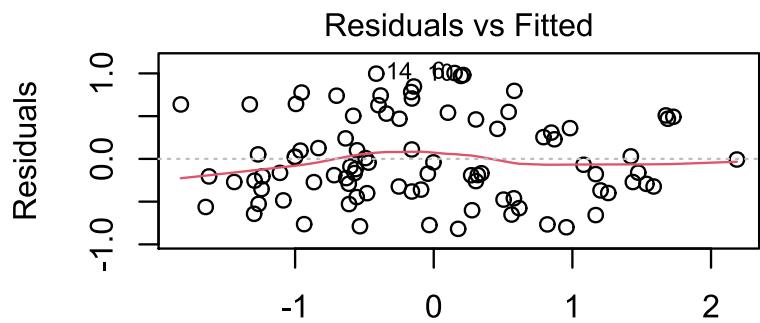
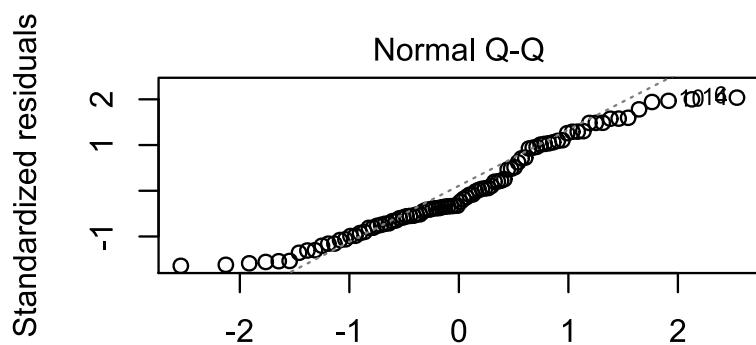


Fig. 4. Quantiles distributions in BGB predicting model of shrubs

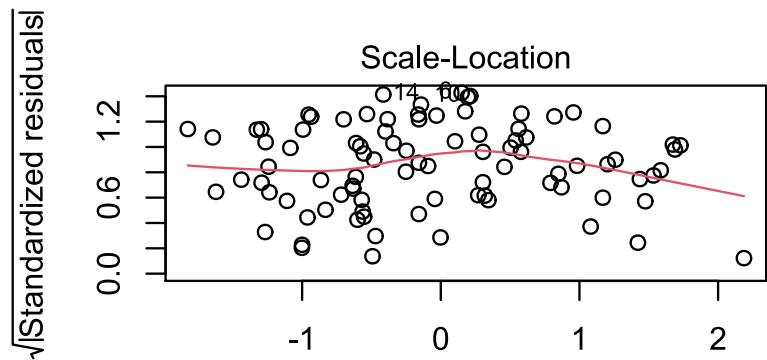
Normal probability (Q-Q) plot and other quantile distributions that assess goodness of fit of the model predicting the total aboveground biomass (BGB) of shrubs as a function of variable $w = \rho D_b^2 H$ and $n =$ the total number of stems for one shrub.



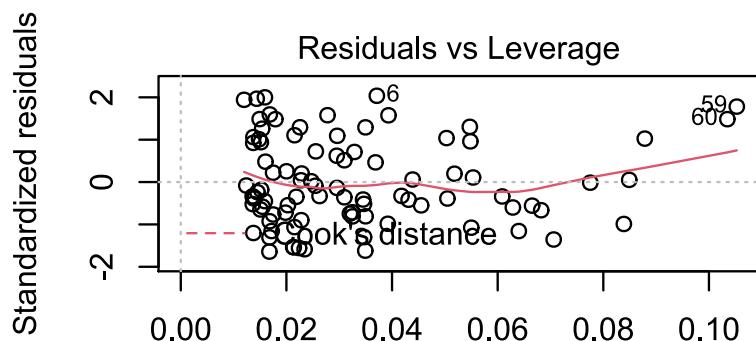
Fitted values
 $\ln(\log(BGB)) \sim \log(rDb2H) + \log(n)$



Theoretical Quantiles
 $\ln(\log(BGB)) \sim \log(rDb2H) + \log(n)$



Fitted values
 $\text{Im}(\log(\text{BGB}) \sim \log(\text{rDb2H}) + \log(n))$



Leverage
 $\text{Im}(\log(\text{BGB}) \sim \log(\text{rDb2H}) + \log(n))$